

Volcanic ash transport using parallel, adaptive Ash3d

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2010 Eyjafjallajökull

The April 15-21, 2010 Eyjafjallajökull eruption in Iceland caused unprecedented disruption to civil European airspace.

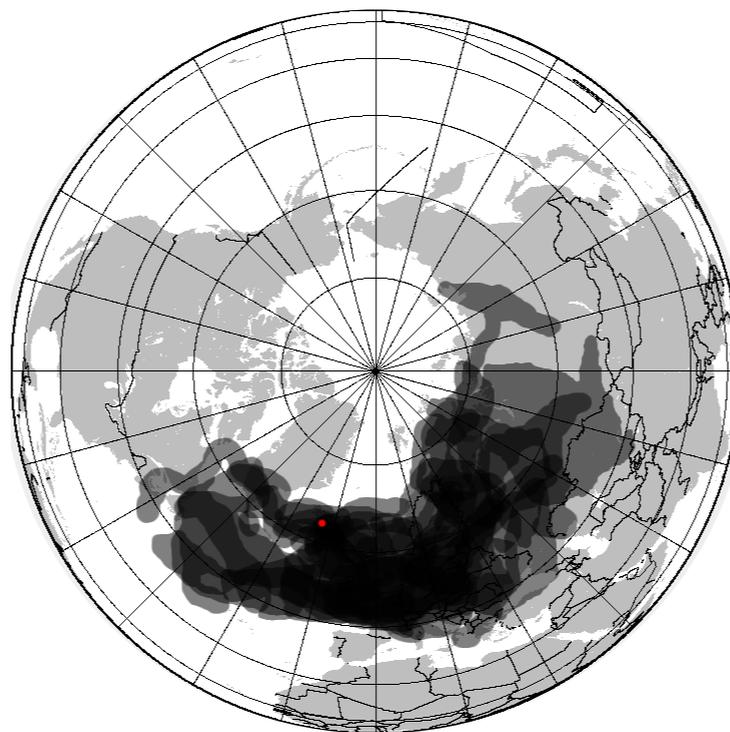
- 25 countries and over 4 million passengers were affected
- Cost to the airlines were measured in the billions of Euros (Oxford-Economics, 2010)

On April 20th, the previous “zero-ash-tolerance” policy were substituted for policies allowing for low level concentrations of ash in commercial airspace.

As a result numerical models must now be able to report ash concentration levels accurately.

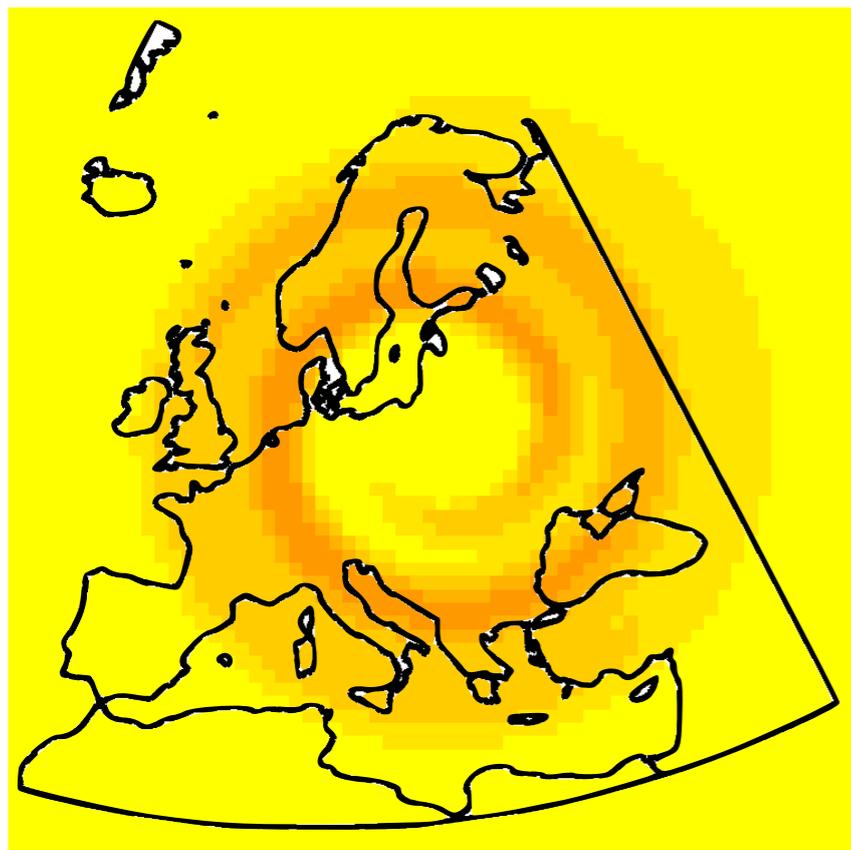
Volcanic eruption 2010

Horizontal scale $\sim O(5000\text{km})$

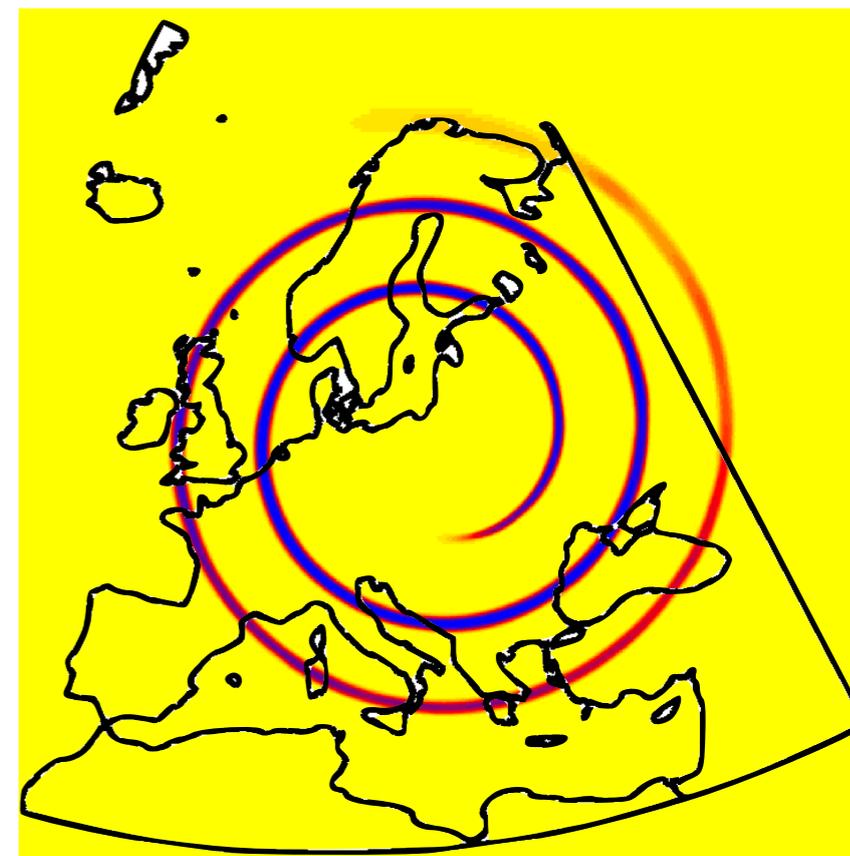


2010 Eruption in Iceland

Evolution has to be tracked over several days



64 x 64 (~ 80 km resolution)



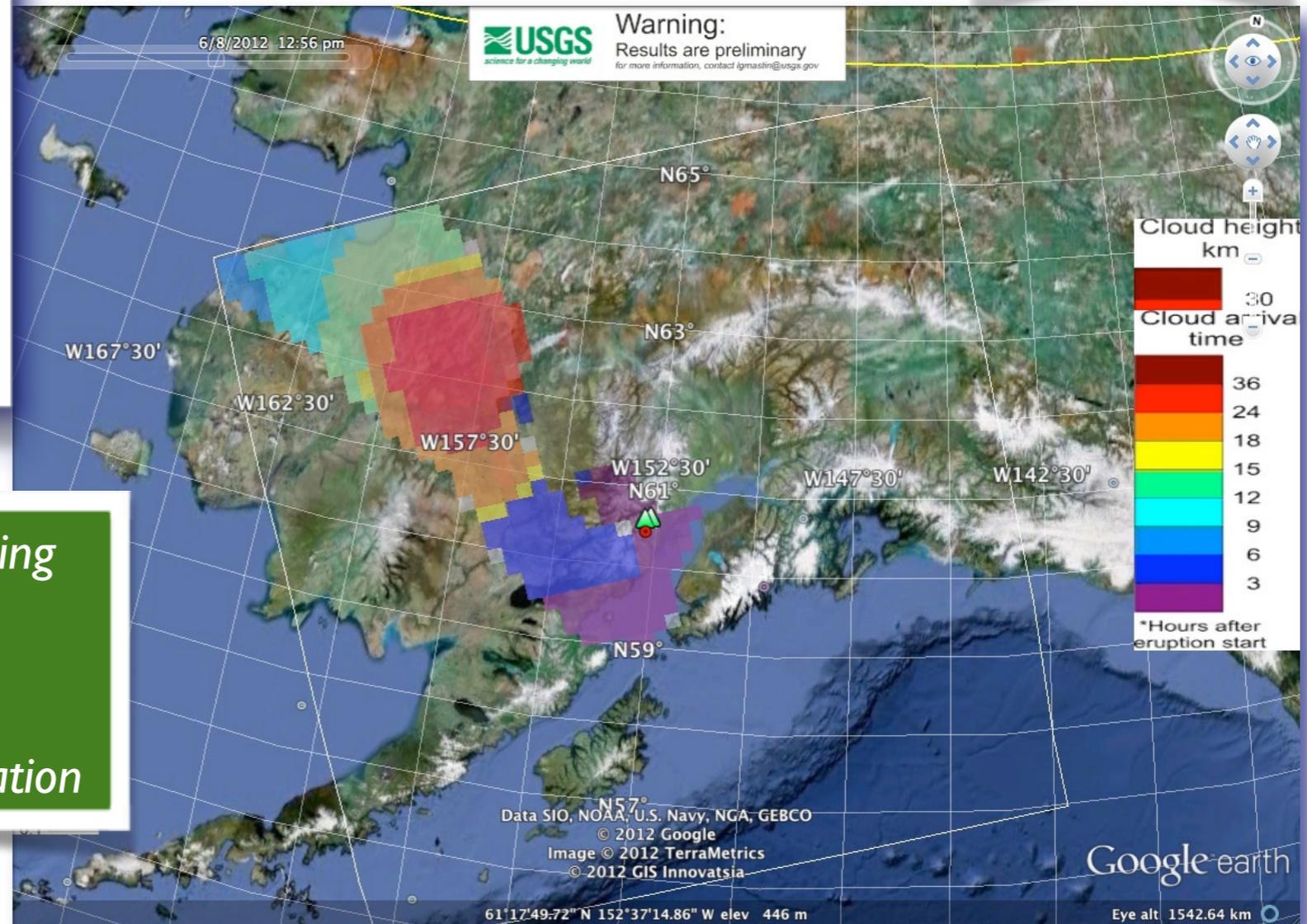
1024 x 1024 (~ 5 km resolution)

Need for high resolution

- Importance of tracking small scale structures in smooth, even coarse-resolution wind fields (Behrens, MWR 2000)
- Observational evidence supports the idea that there is considerable variation in concentration levels in tracers in the atmosphere, not just large diffuse “clouds” of tracers.
- Eruptions lasting several days or weeks can place heavy demands on computational resources.

Ash 3d : Ash cloud modeling

Ash3d



- Split horizontal, vertical time stepping
- Fully conservative,
- Eulerian, finite volume
- Algorithms based on wave propagation

Ash3d :A finite-volume, conservative numerical model for ash transport and tephra deposition, Schwaiger, Denlinger, Mastin, JGR (2012)

Ash3d

The scalar advection equation in conservative form

$$q_t + \nabla(\mathbf{u}q) = \Psi(q)$$

where the velocity field \mathbf{u} is prescribed from wind field data available from various weather services (e.g. NOAA) and q is a concentration of ash. One or more grain sizes may be tracked.

- Use high-resolution wave propagation algorithms
- Variable-coefficient advection problem raises interesting issues (potential loss of hyperbolicity near sonic points, for example).
- Source term models eruption using one of several well-established models

Ash3d

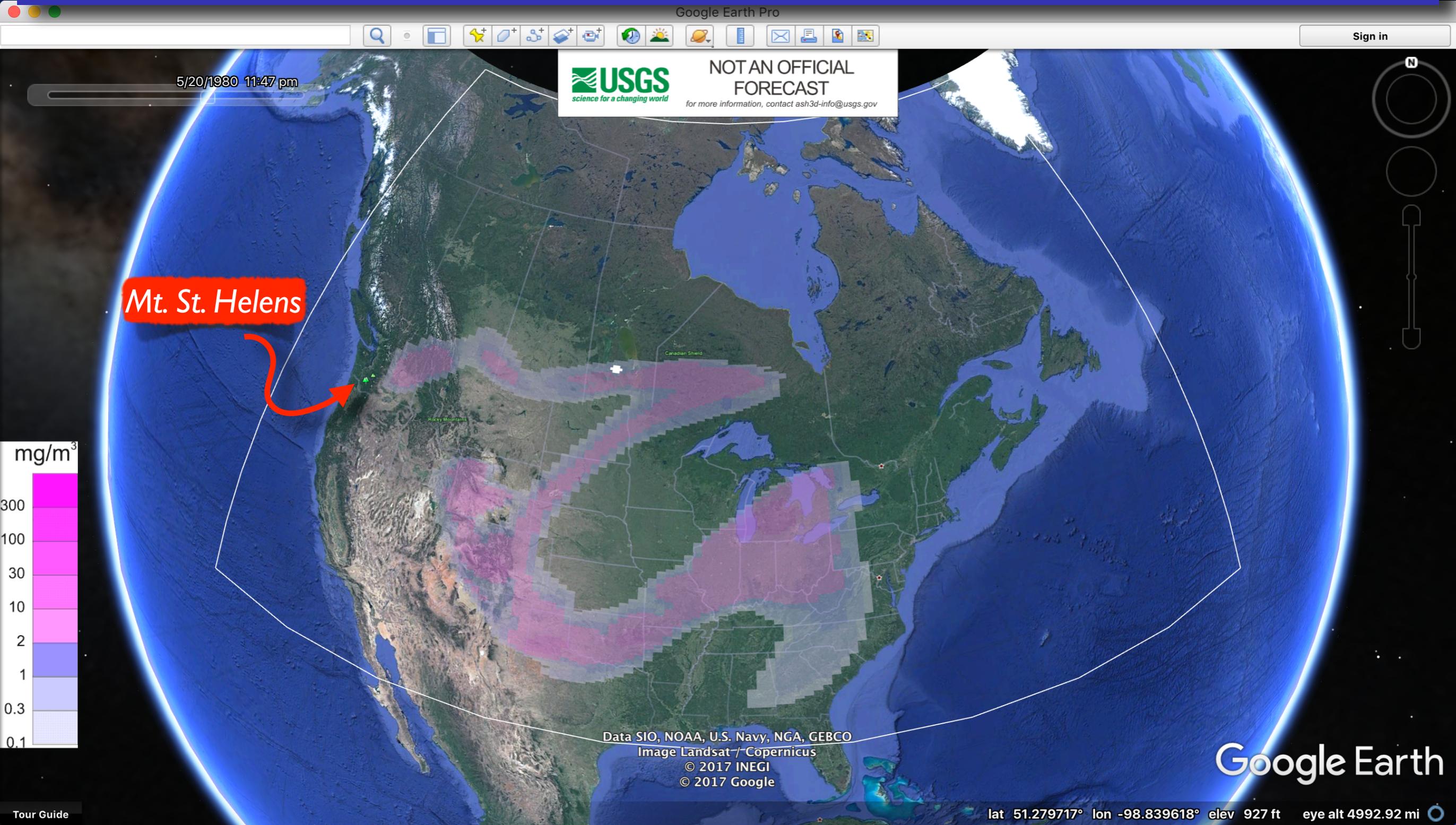
Computational domain

- Regional finite volume, lat-long grid
- 3d computations, with roughly 25 cells in the vertical.
- Runs on a single processor (serial code)
- Wind fields interpolated in space and time from forecast (or re-analysis) data.

Numerical formulation

- Explicit finite volume scheme with wave limiters (ala Clawpack)
- Eulerian formulation ensures conservation of ash mass,
- Conservative discretization designed to preserve second order accuracy

Ash3d Results



ForestClaw Project

A parallel, adaptive library for logically Cartesian, mapped, multi-block domains

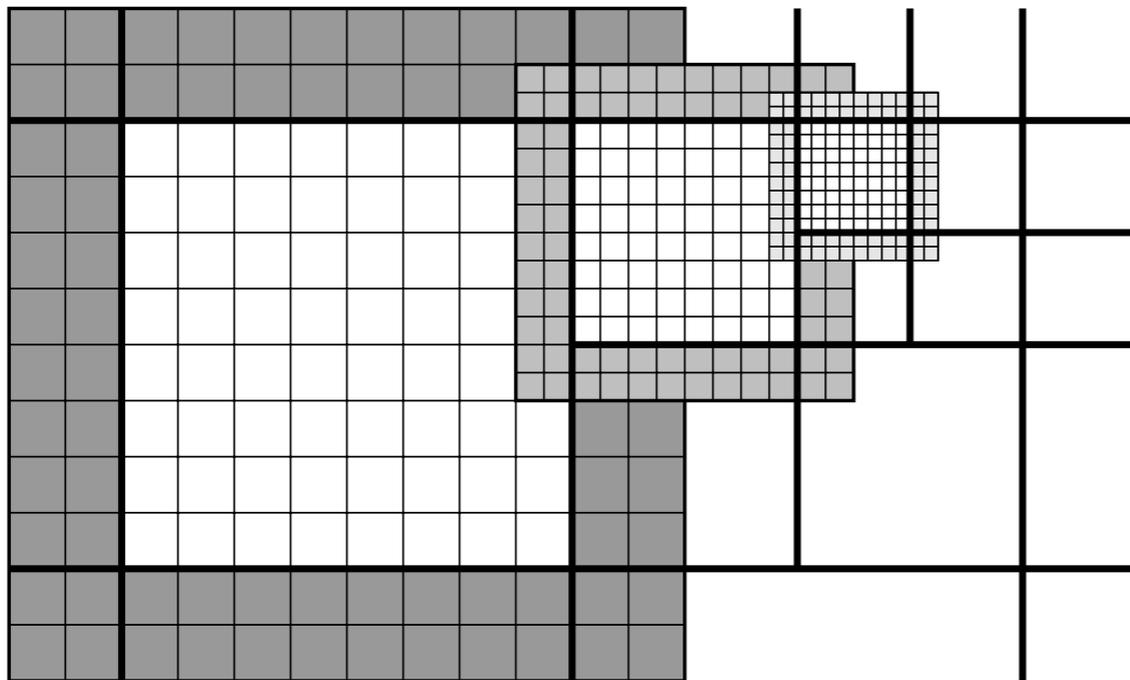
Features of ForestClaw include :

- Uses the **highly scalable p4est** dynamic grid management library (C. Burstedde, Univ. of Bonn, Germany)
- Each leaf of the quadtree contains a fixed, uniform grid,
- Optional multi-rate time stepping strategy,
- Has **mapped, multi-block** capabilities, (cubed-sphere, for example) to allow for flexibility in physical domains,
- Modular design gives user flexibility in extending ForestClaw with Cartesian grid based solvers and packages.
- Uses essentially the same algorithmic components as patch-based AMR

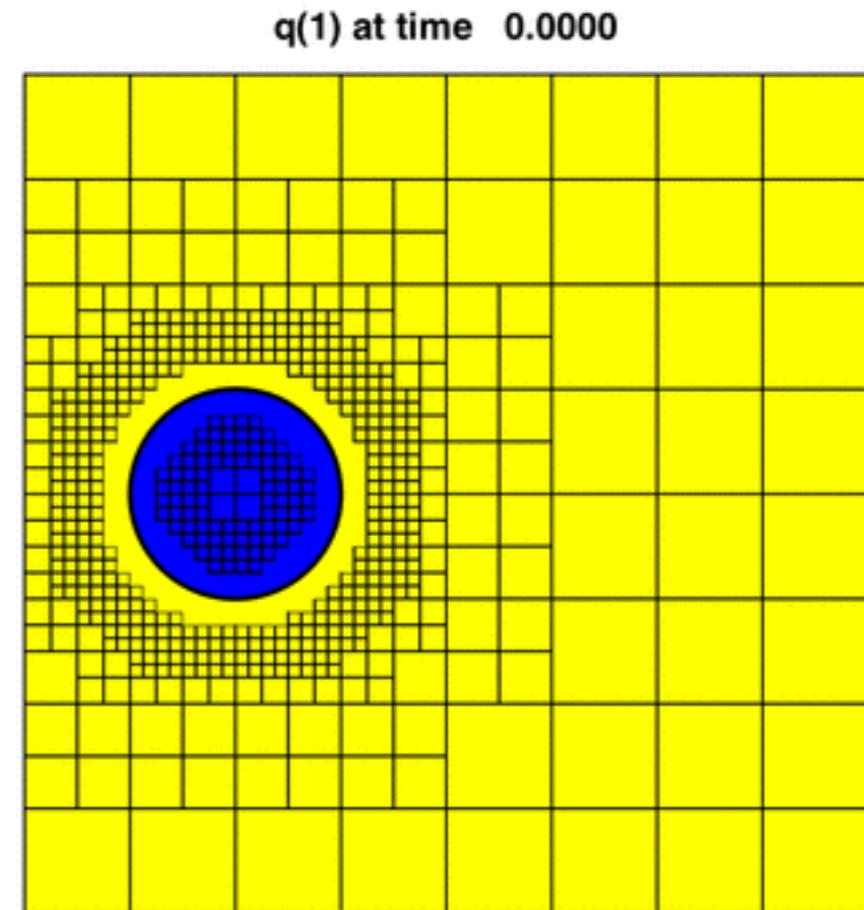
Thanks to NSF for supporting this work

www.forestclaw.org

ForestClaw adaptivity



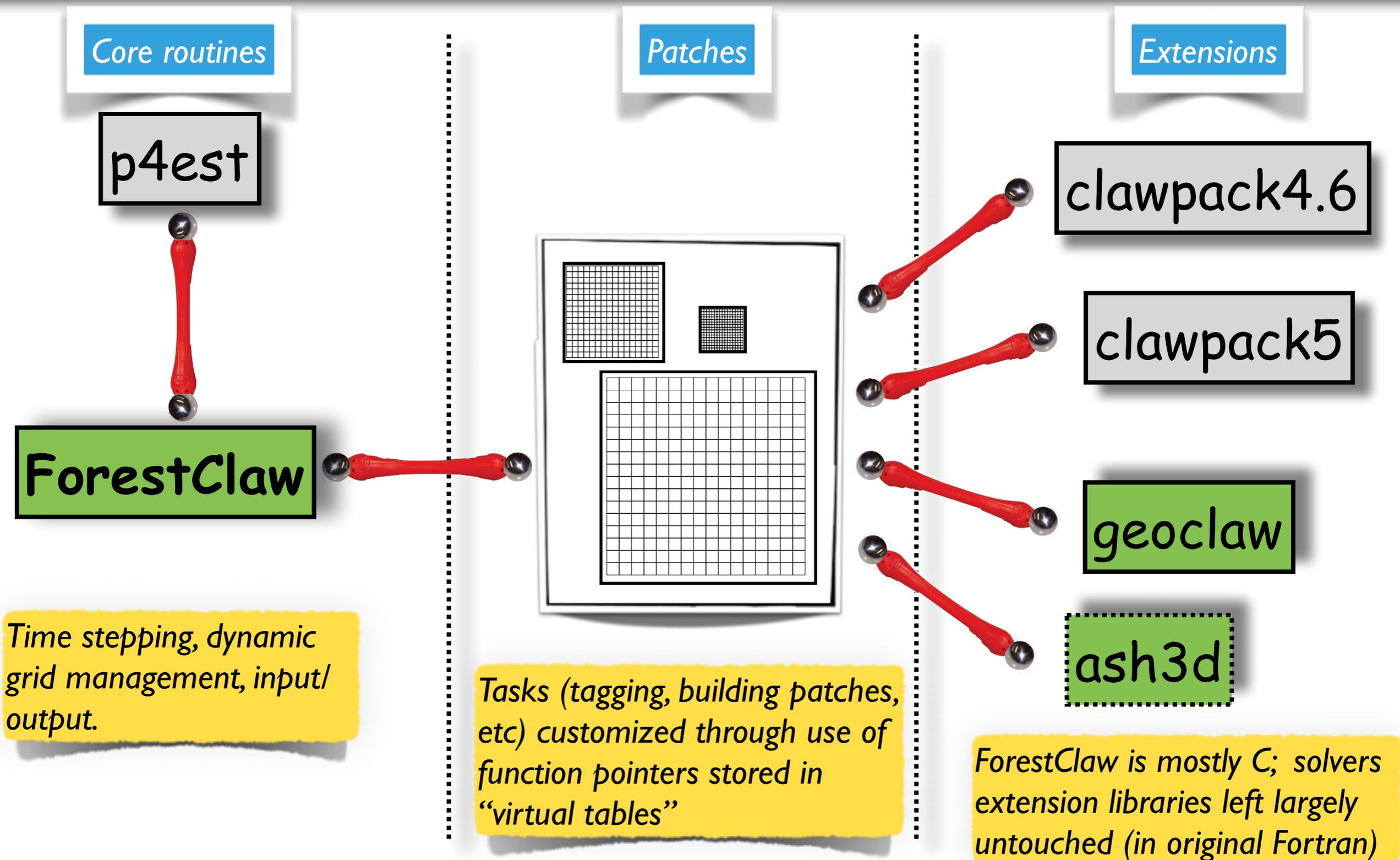
Each quadrant is a single logically grid, designed for finite volume or finite difference solvers.



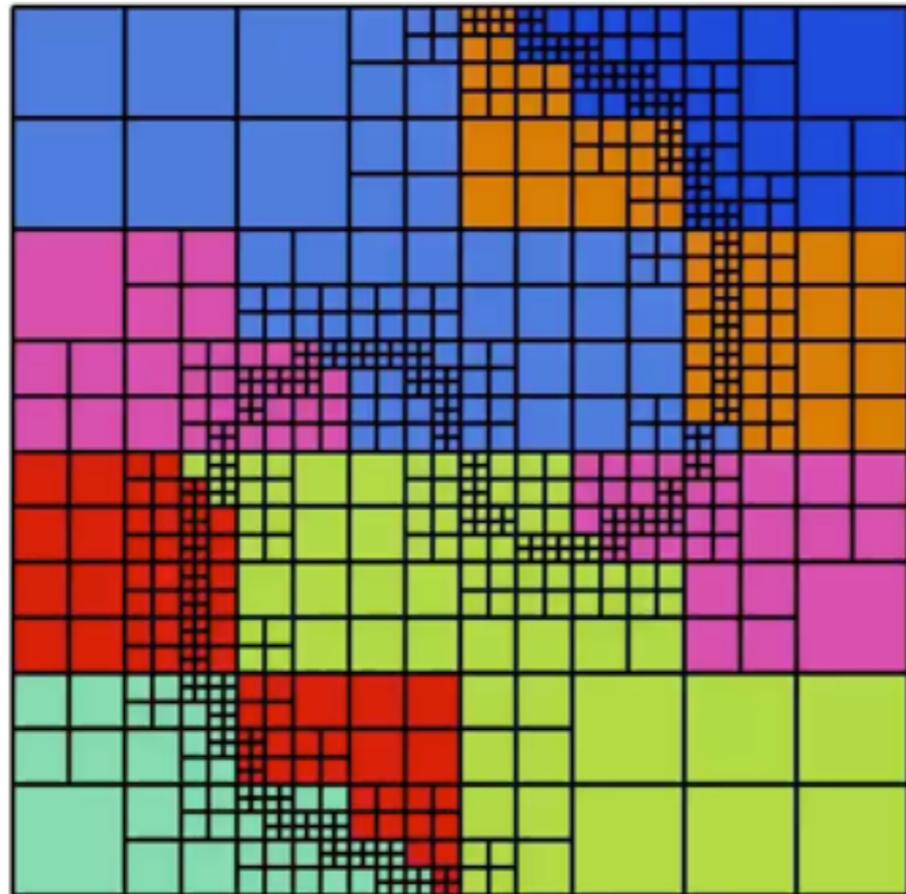
(Behrens, MWR 2000)

Regridding, connectivity done using p4est (www.p4est.org)

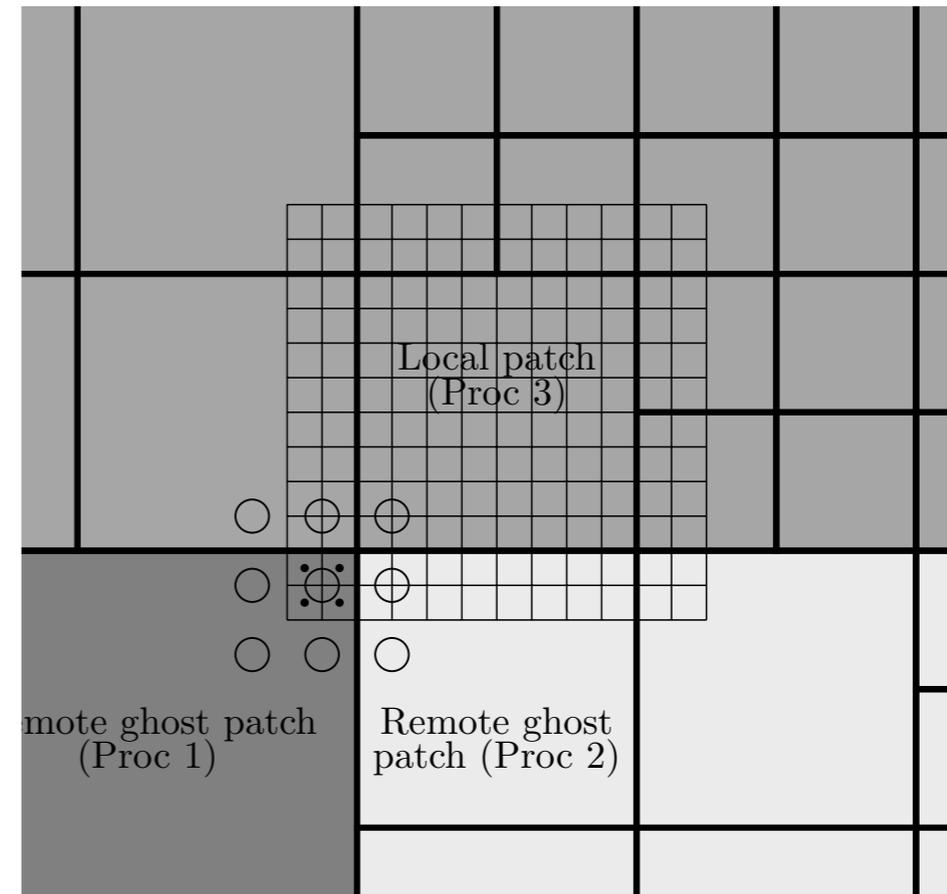
Extending ForestClaw



ForestClaw - Parallelism



p4est : Load balancing using a space filling curve

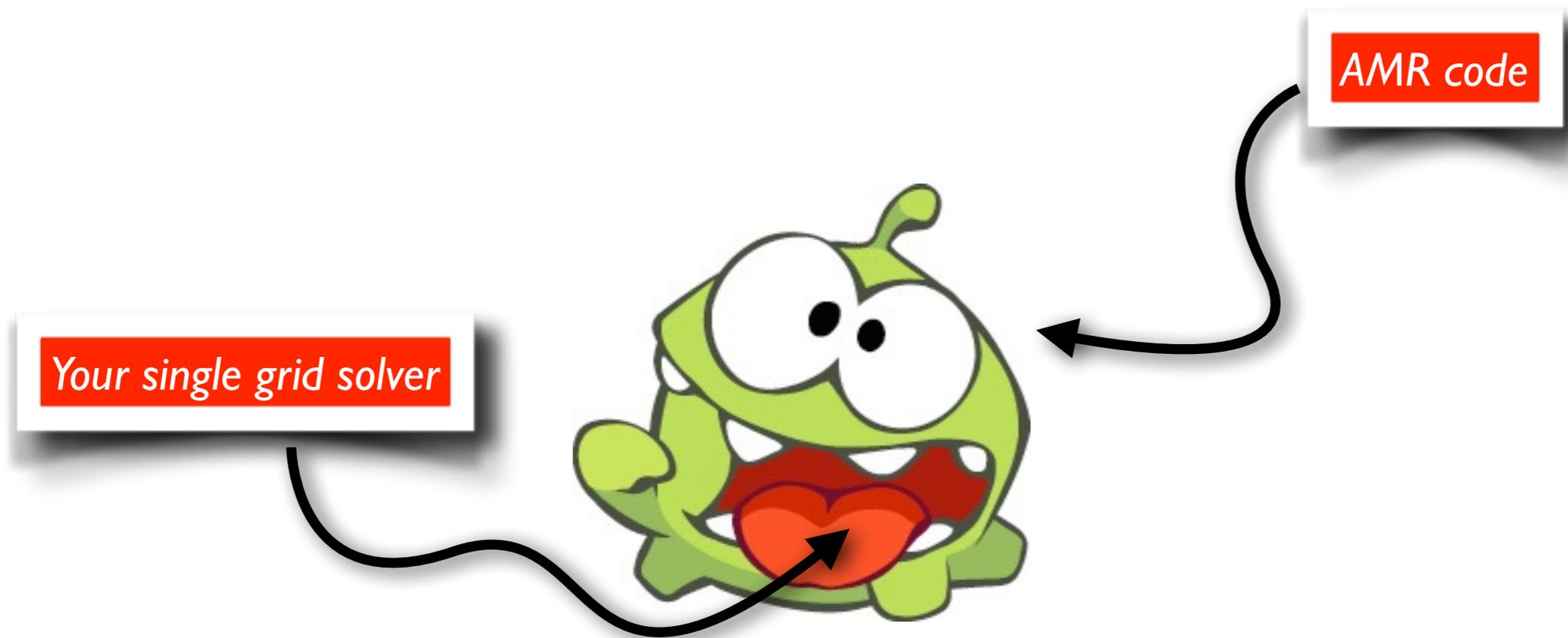


Fine grid corner ghost cells at corners where 3 or more processors meet

D. Calhoun and C. Burstedde, "ForestClaw : A parallel algorithm for patch-based adaptive mesh refinement on a forest of quadtrees", (submitted), 2017. ([arXiv:1703.03116](https://arxiv.org/abs/1703.03116))

AMR ?

Mental model of how this might work :



* Idea for code name : OmNum

Block-structured AMR

The Dream

```
AMR.run(max_time, max_steps);
```

*Your single grid solver
is called from here.*



Block-structured AMR

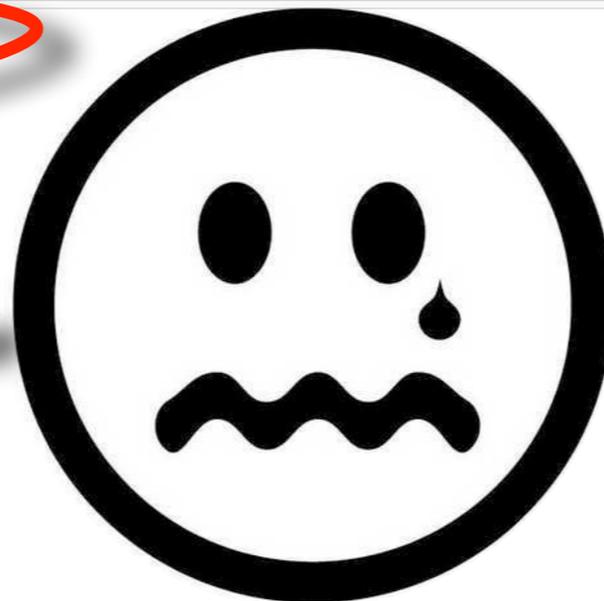
The Reality

```
Tuple< RefCountedPtr<AMRLevelOpFactory<
LevelData<FArrayBox> > >, SpaceDim> velTGAOpFactoryPtrs;

for (int idir = 0; idir < SpaceDim; idir++)
{velTGAOpFactoryPtrs[idir] =
  RefCountedPtr<AMRLevelOpFactory<LevelData
<FArrayBox> > >
  ((AMRLevelOpFactory<LevelData<FArrayBox> >*)
  (new AMRPoissonOpFactory())); //.....
```

Your single grid solver

you



Retro...

```
node (ndjhi ,mptrnx) = node (ndjhi ,mptr)
node (ndjhi ,mptr)   = node (ndjlo ,mptr) + nyl - 1
node (ndjlo ,mptrnx) = node (ndjhi ,mptr) + 1
node (ndihi ,mptrnx) = node (ndihi ,mptr)
node (ndilo ,mptrnx) = node (ndilo ,mptr)

rnode (cornxlo ,mptrnx) = cxlo
rnode (cornylo ,mptrnx) = cymid
rnode (cornyhi ,mptrnx) = cyhi
rnode (cornxhi ,mptrnx) = cxhi
node (nestlevel ,mptrnx) = node (nestlevel ,mptr)
rnode (timemult ,mptrnx) = rnode (timemult ,mptr)
go to 10
```



Ash3d - Fortran modules

```
MODULE ash3d
  REAL(kind=8), ALLOCATABLE :: concen(:, :, :, :)
  !! ...
END
```

```
SUBROUTINE allocate()
  USE ash3d
  IMPLICIT NONE

  ALLOCATE (concen(0:n+1, 0:n+1, 0:n+1, 2))
  !! ...
END
```

Original code: Single grids allocated at start of run

```
SUBROUTINE update_concen()
  USE ash3d
  IMPLICIT NONE

  concen(:, :, :, 1) = concen(:, :, :, 0) + dt*(your favorite scheme)
  !! ...
END
```

Ash3d - Fortran modules

```
struct patch
{
    double *concen;
    /* ... + 30 more arrays */
};
```

```
void init_patch(patch* p)
{
    allocate_();
    store_ptrs_(&p->concen);
}
```

```
void update(patch* p)
{
    copy_ptrs2mod_(p->concen);
    update_concen_();
}
```

Original code

```
MODULE ash3d
REAL(kind=8), POINTER :: concen(:, :, :, :)
INTEGER(KIND=4) :: n
!! ... + 30 more arrays !!
END
```

```
SUBROUTINE allocate()
    USE ash3d
    IMPLICIT NONE

    ALLOCATE(concen(0:n+1, 0:n+1, 0:n+1, 2))
END
```

```
SUBROUTINE update_concen()
    USE ash3d
    IMPLICIT NONE

    concen(:, :, :, 1) = concen(:, :, :, 0) &
        + dt*(your favorite scheme)
END
```

```
SUBROUTINE store_ptrs(fc_concen_ptr)
    USE iso_c_binding
    USE ash3d
    IMPLICIT NONE

    TYPE(C_PTR) :: fc_concen_ptr

    fc_concen_ptr = C_LOC(concen)
END
```

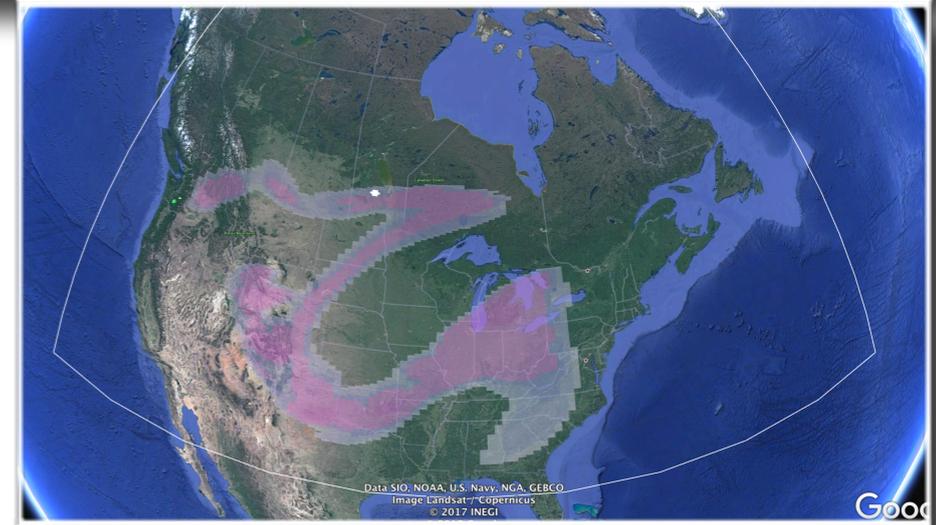
```
SUBROUTINE copy_ptrs2mod(fc_concen_ptr)
    USE iso_c_binding
    USE ash3d
    IMPLICIT NONE

    TYPE(C_PTR) :: fc_concen_ptr
    REAL(KIND=8), POINTER :: ptr(:)

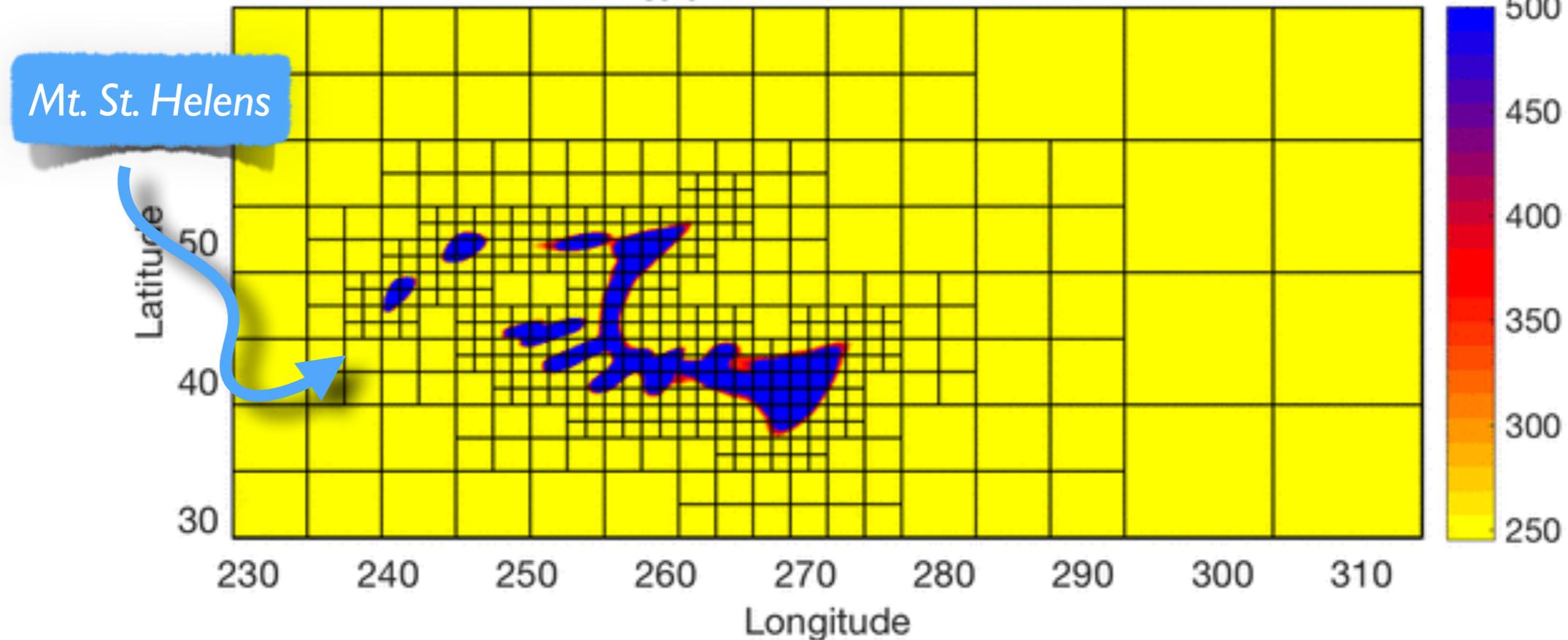
    CALL C_F_POINTER(fc_concen_ptr, ptr, [1])
    concen(0:n+1, 0:n+1, 0:n+1, 2) => ptr
END
```

Adaptive Ash3d

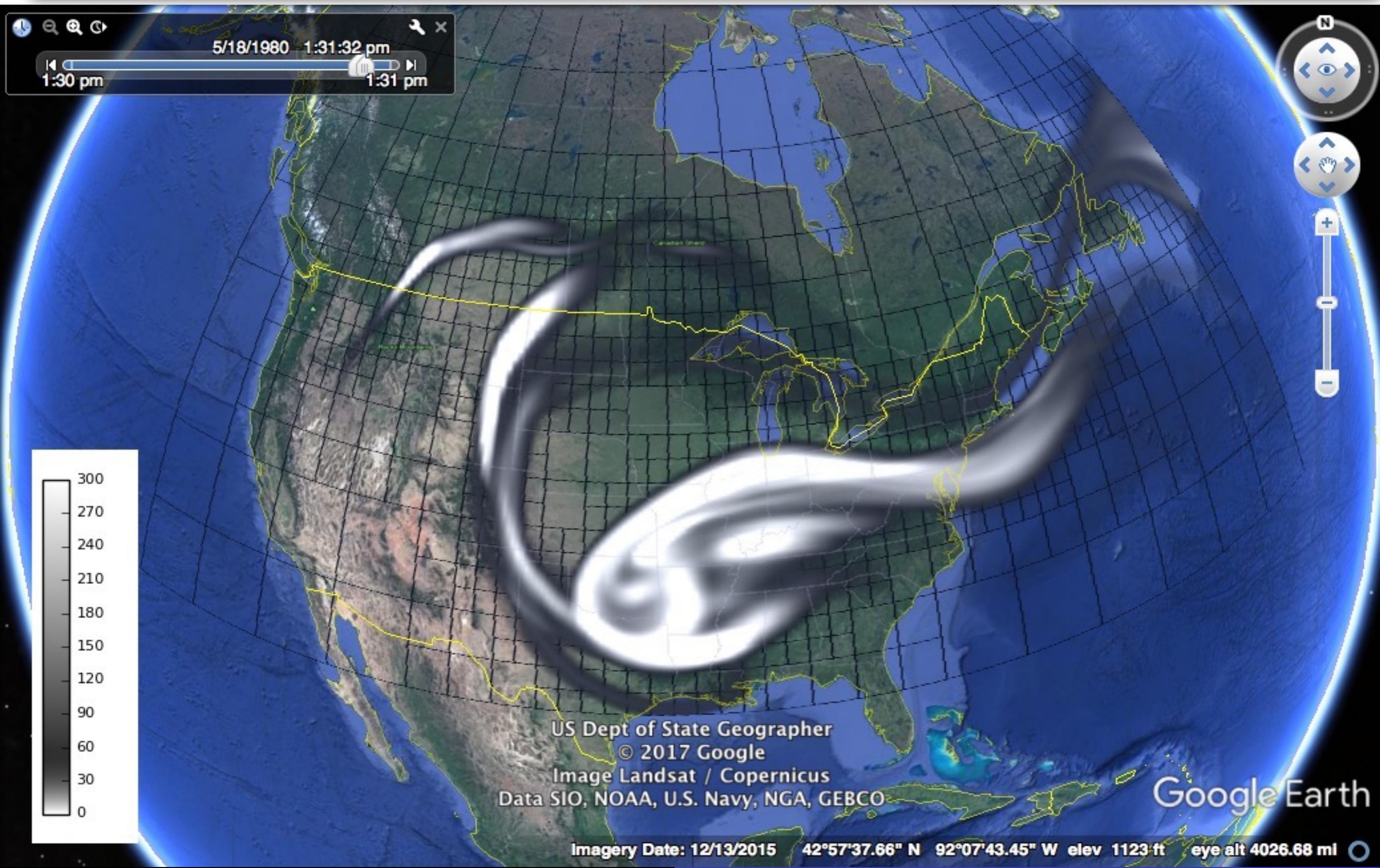
- 96 hour simulation
- 1024 x 512 effective resolution
- 3-4 times faster than single grid



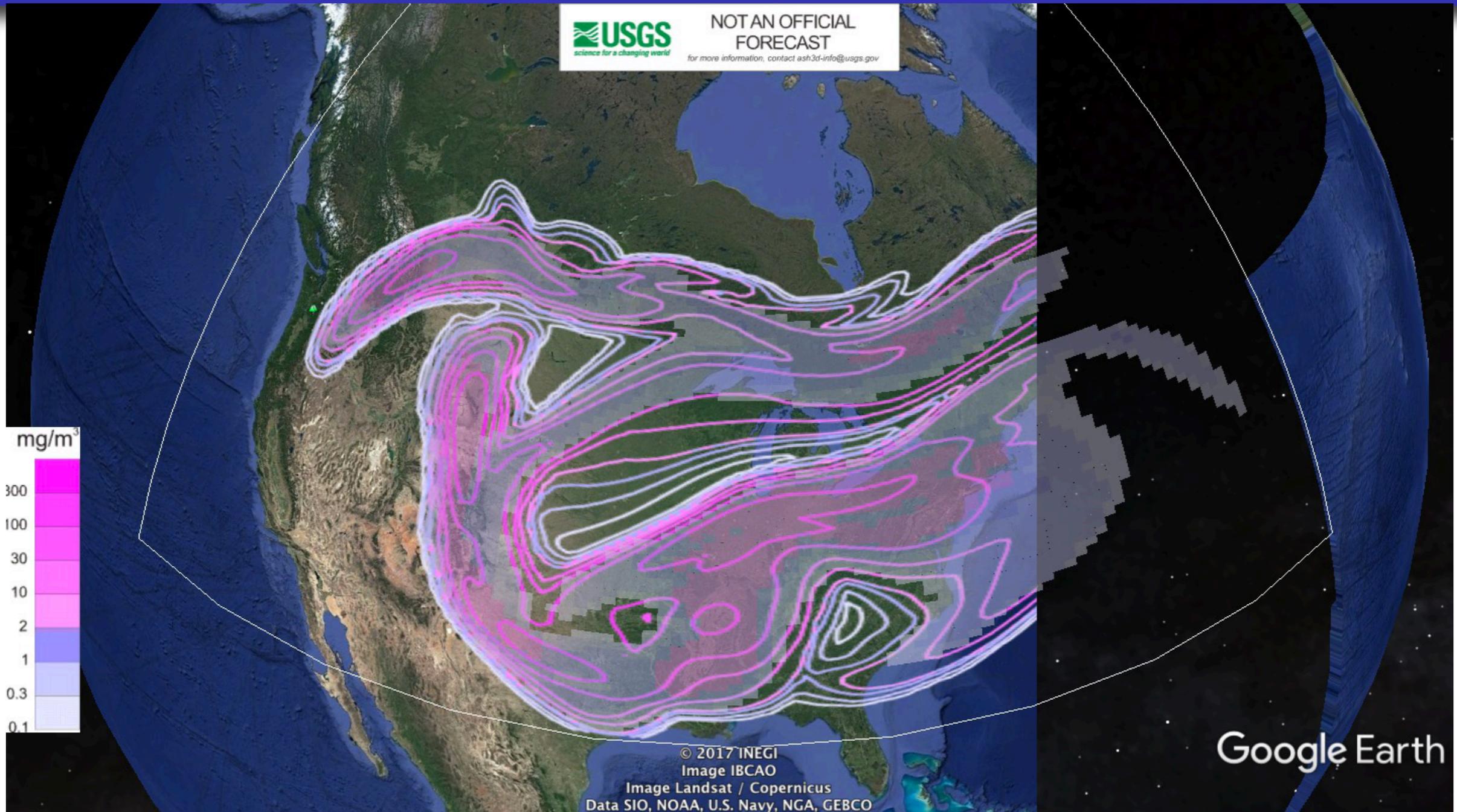
q(1) at time 40.0000



Adaptive results

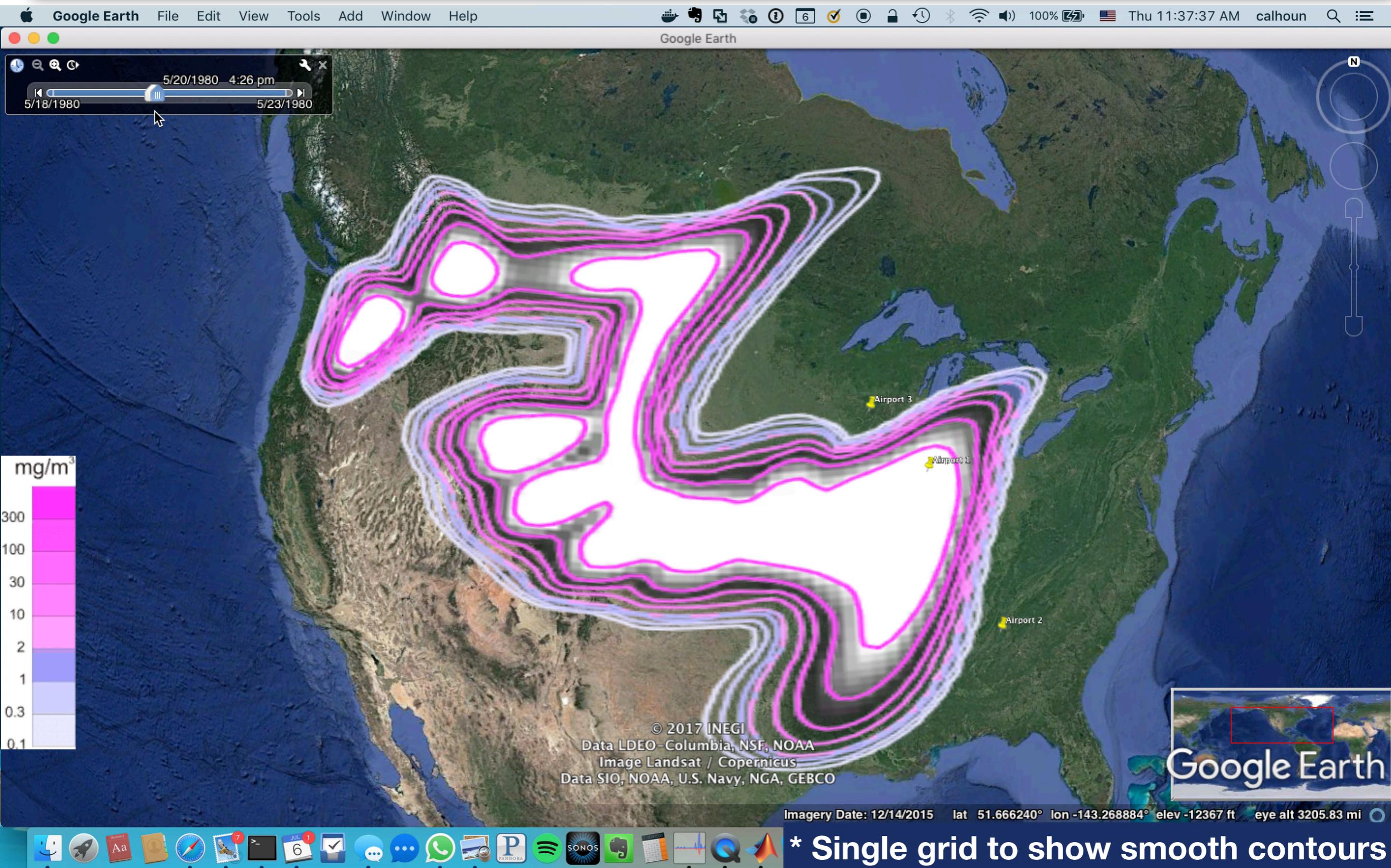


Single grid comparison

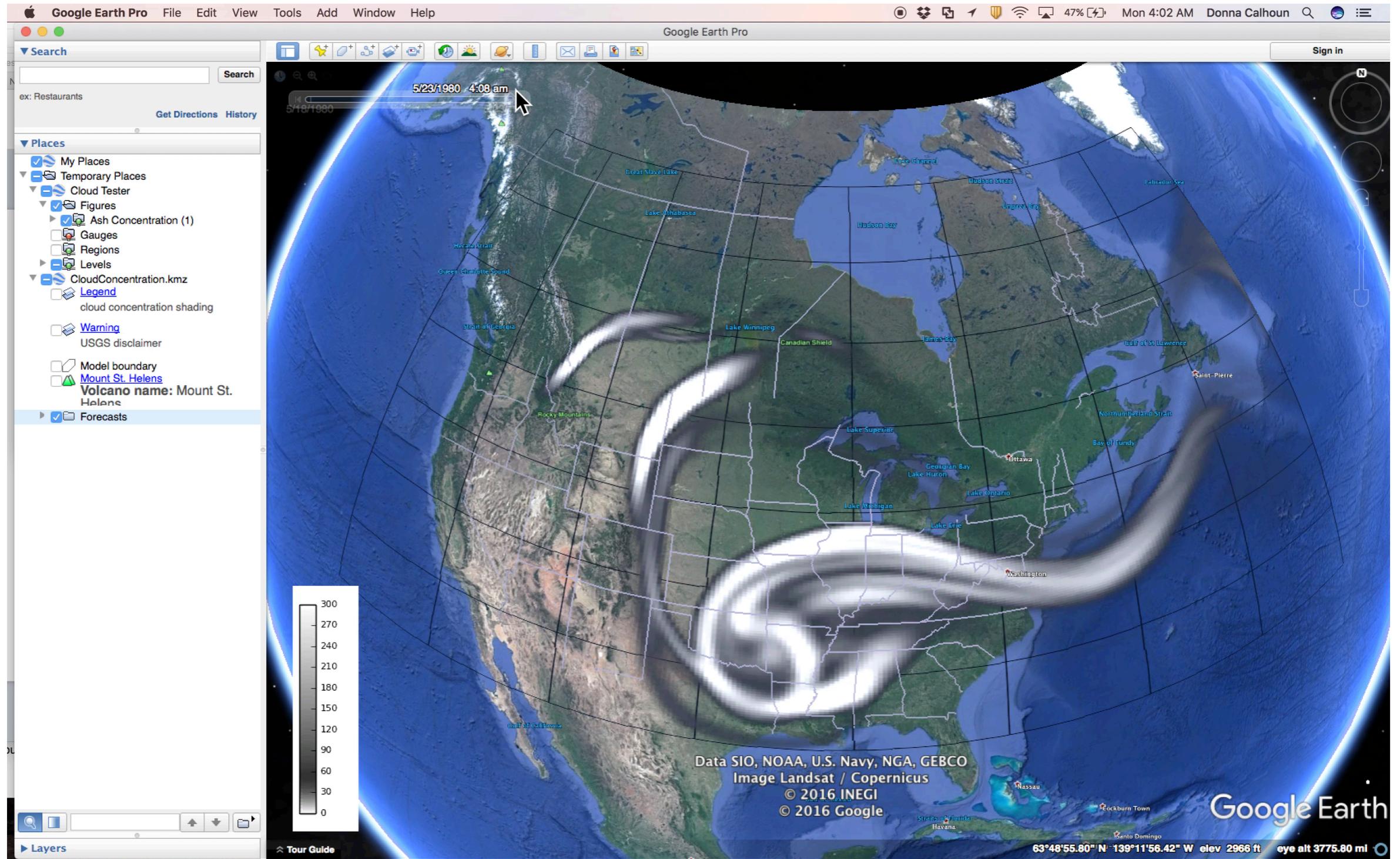


- Comparison between original Ash3d (pcolor plot) and ForestClaw (contours).
- Calculations done on a single 128x128 grid

Single grid comparison

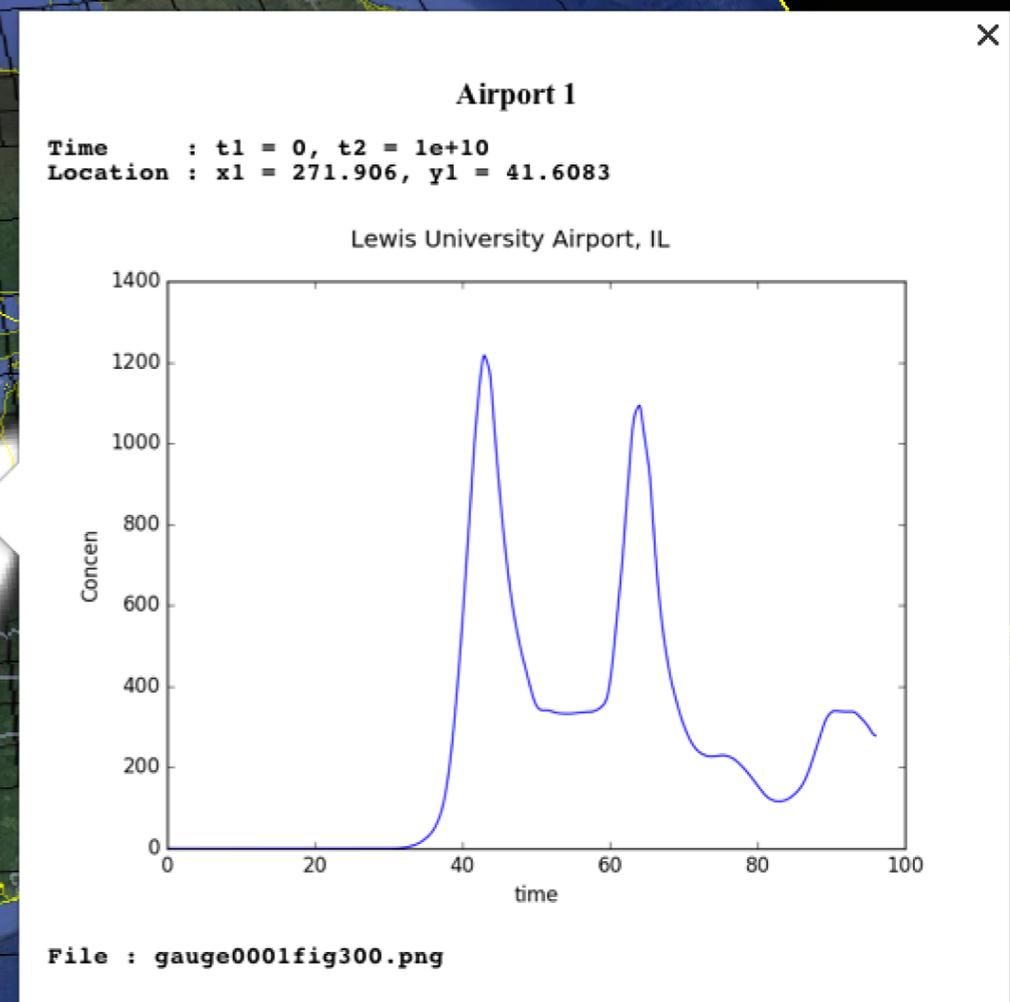
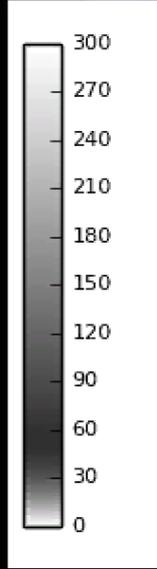


Single grid comparison



Airports

5/20/1980 3:36 pm

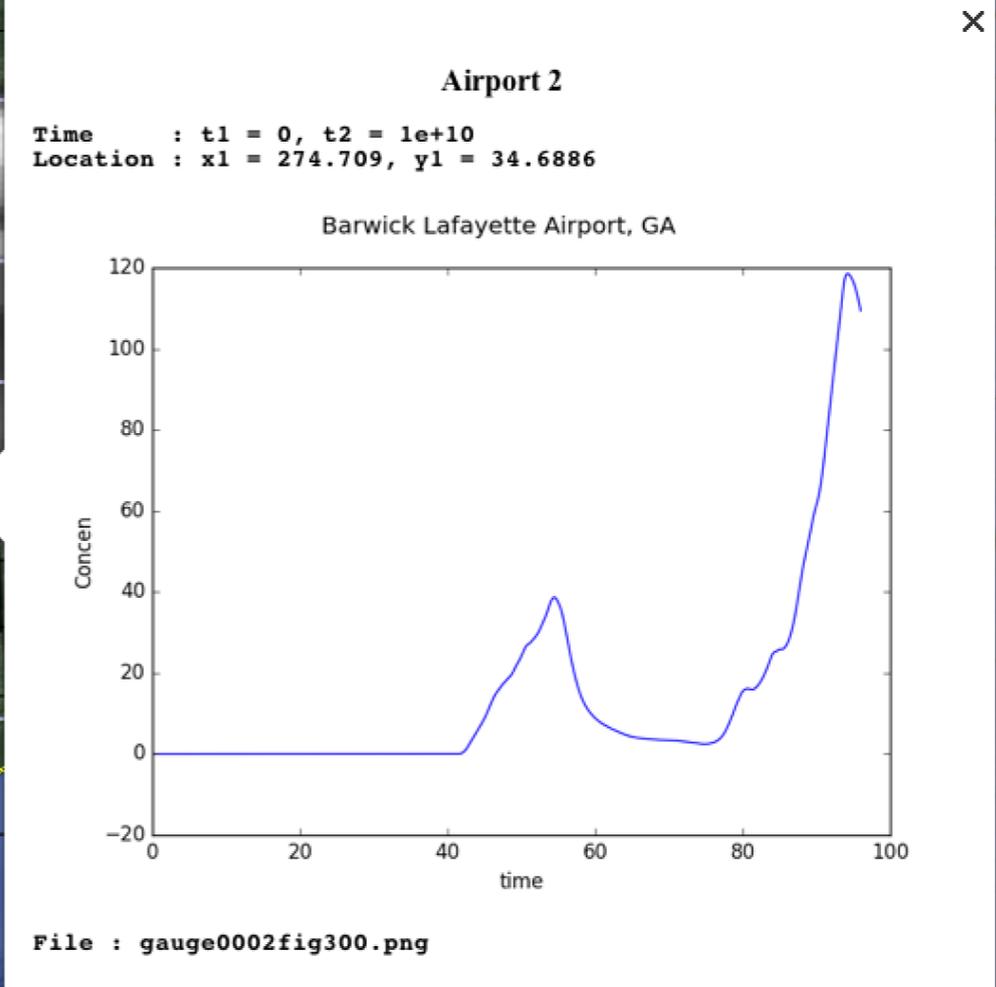
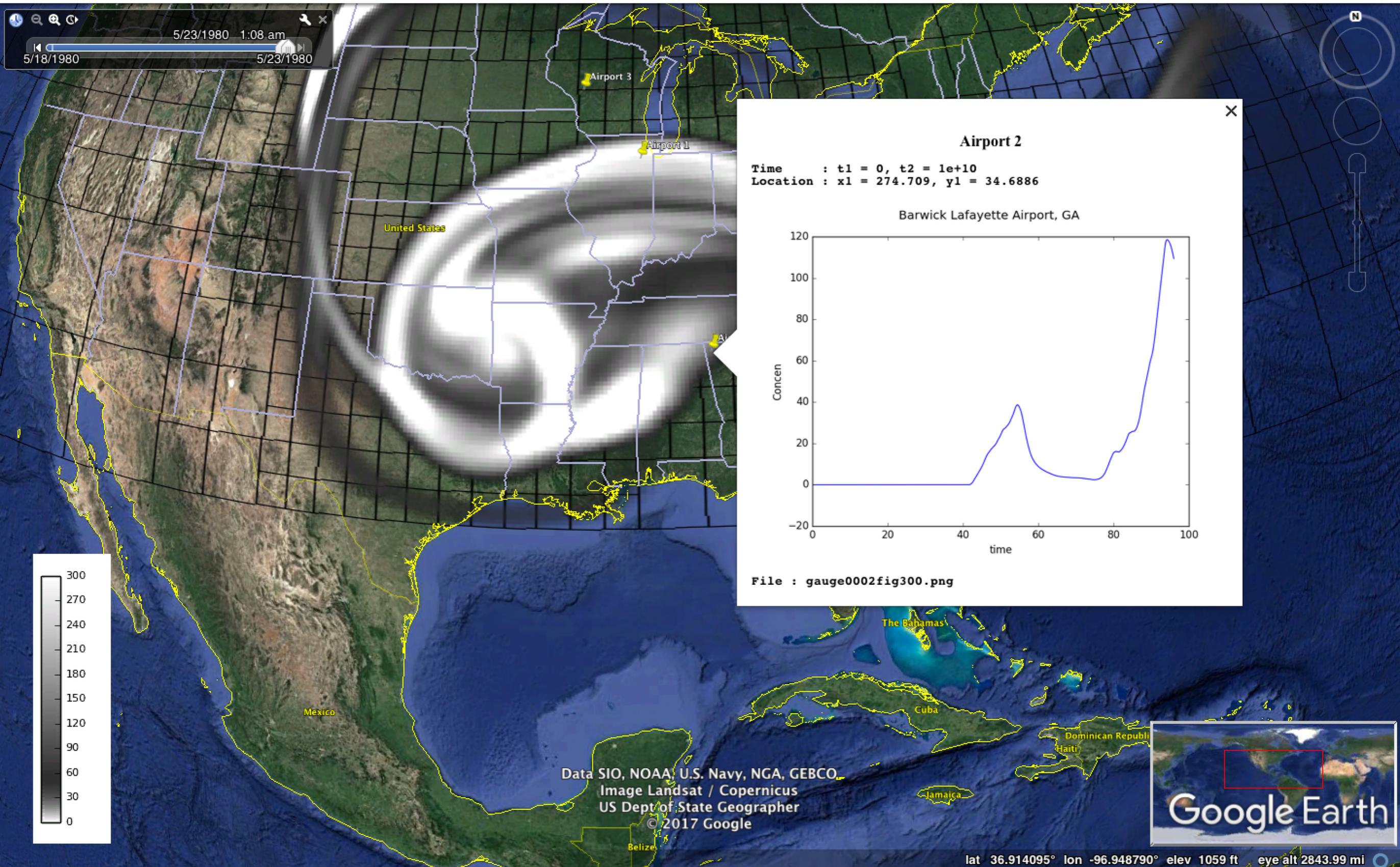


Data SIO, NOAA, U.S. Navy, NGA, GEBCO
Image Landsat / Copernicus
US Dept of State Geographer
© 2017 Google

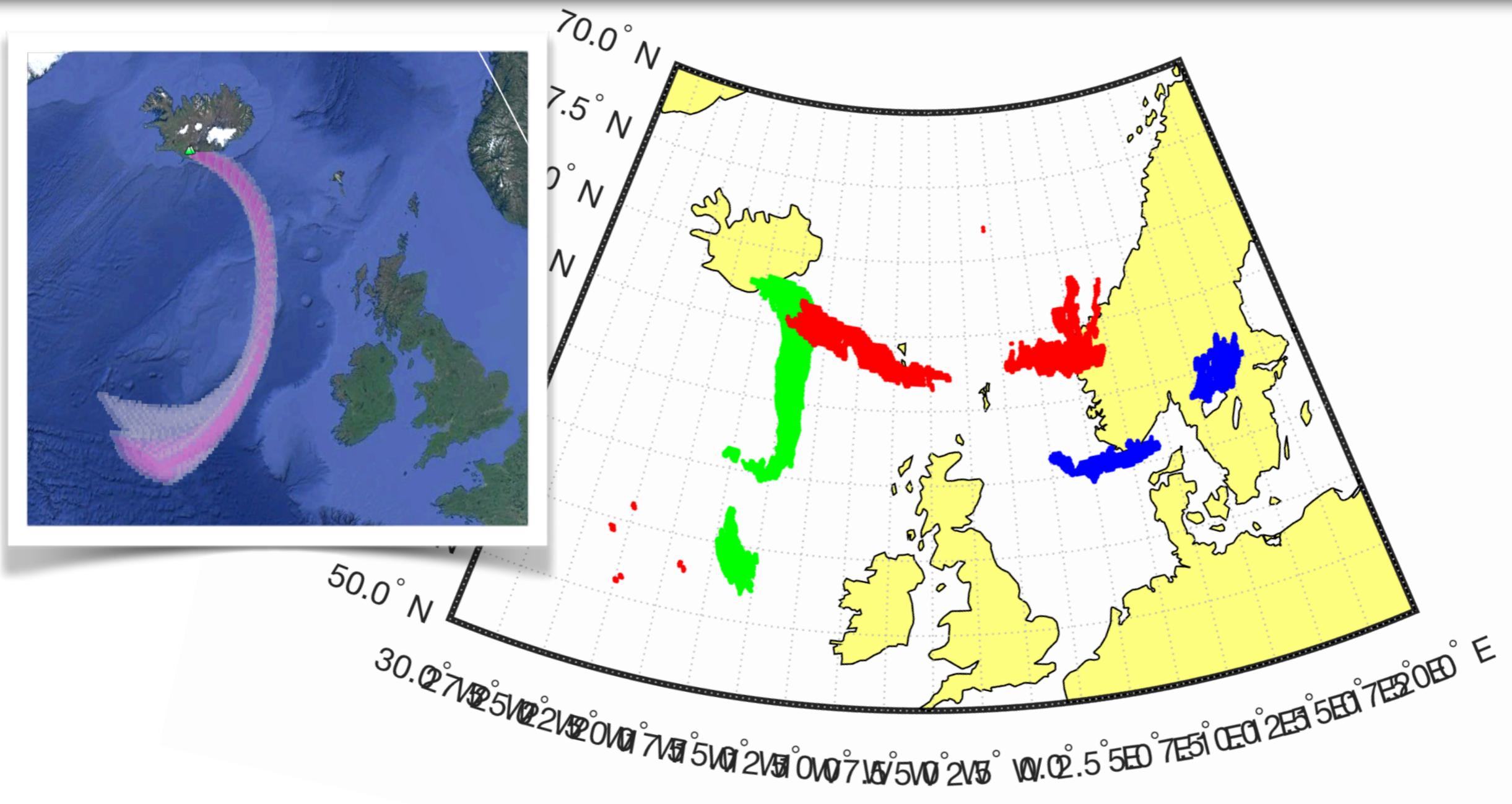


lat 41.921113° lon -87.741316° elev 589 ft eye alt 4650.43 mi

Airports



Iceland (satellite data)



Satellite data available for comparison

Future plans

- Extend to cubed sphere grid for problems over the poles (difficult with lat-long grids)
- Consider other numerical schemes to handle conservation (f-waves, for example).
- Performance testing, and effects of IO

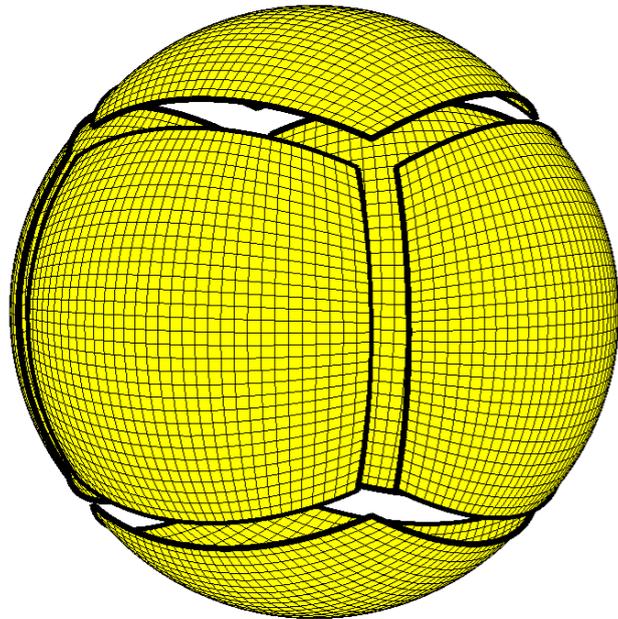
Tracer transport is an important component in larger weather and climate models and can often take up the majority of the computational time

- Other transport problems : smoke, pollution, vapor, CO₂, and so on.

www.forestclaw.org

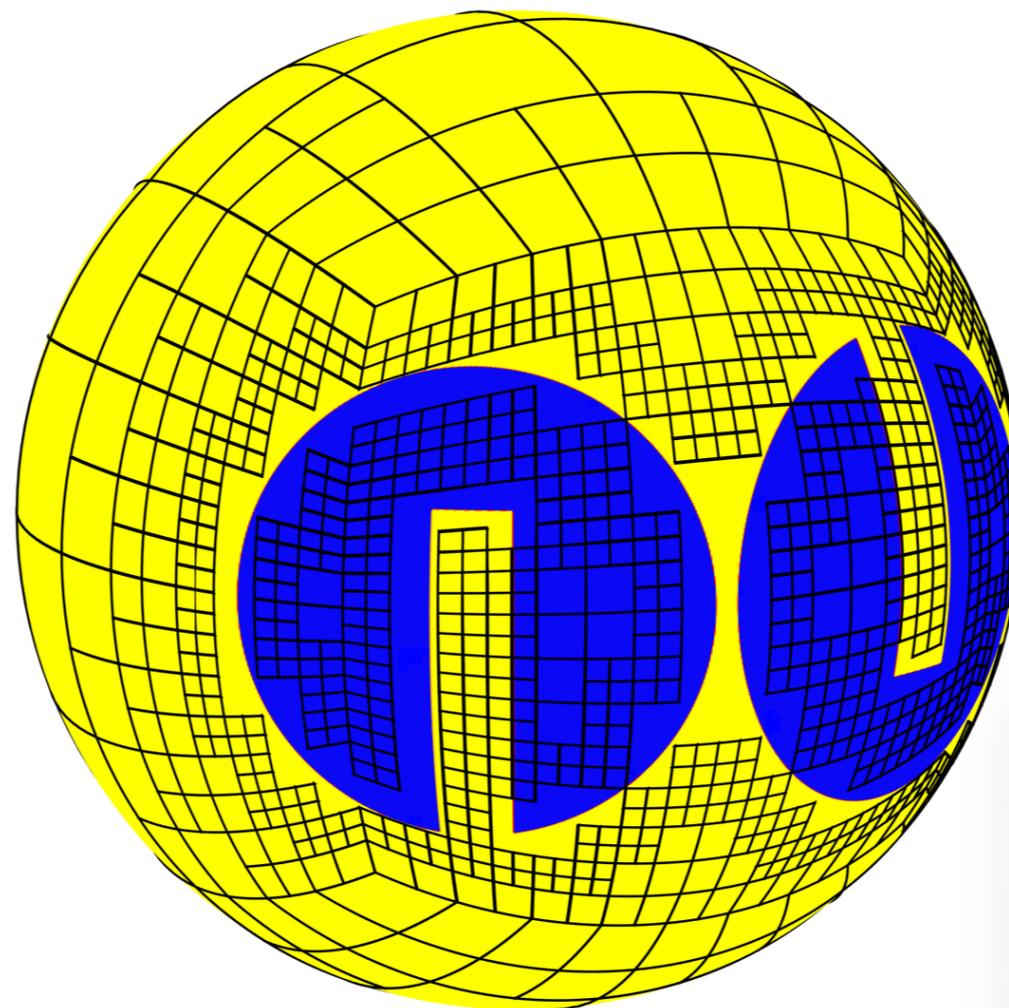
www.github.com/ForestClaw

ForestClaw cubed sphere mesh

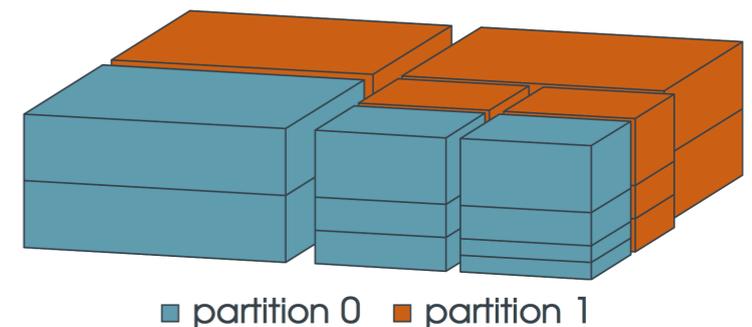


Cubed sphere
grid in ForestClaw

q(1) at time 0.0000



Horizontal scale $\sim O(1000\text{km})$
Vertical scale $\sim O(10\text{km})$



Extrude cubed-sphere to 3d and use p6est (T. Isaac)